Table 4 (cont.)

H & L FCBS FCAL	H K L FLOS FCAL	H K L FEES FEAL	H K L FCUS FCAL	H K L FCOS FCAL	H K L FCBS FCAL	H K L FLMS FCAL	+ K L FCOS FCAL	H F L FCBS FCAL	H K L FOON FCAL
1   2   4   1	$\begin{array}{c} \mathbf{r} & \mathbf{r} & \mathbf{r} \\ \mathbf{r} \\ \mathbf{r} & \mathbf{r} \\ $	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	q   4.5   4.5   8.5   3.5     q   5.4   5.5   5.1   1.1   1.1     q   5.4   5.5   5.1   1.1   1.1   1.1     q   5.4   5.5   5.1   1.1   1.1   1.1   1.1     q   5.5   5.5   5.1   1.1	$ \begin{array}{c} c & s & s_{1} \\ c & s & s_{2} \\ c & s & s_{1} \\ c & s & s_{2} \\ c & s & s_{2} \\ c & s & s_{1} \\ c & s & s_{2} \\ c & s $	$ \begin{array}{c} 13 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $			12   2   3   1	13 3 - 3 - 4 - 4 - 5 - 3 - 7 - 4 - 5 - 5 - 7 - 4 - 5 - 5 - 7 - 7 - 7 - 7 - 7 - 7 - 7 - 7

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# The Refinement of the Crystal Structures of $\beta$ -D-Glucose and Cellobiose

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The structures of  $\beta$ -D-glucose and cellobiose have been refined anisotropically from new data obtained at room temperature with Cu  $K\alpha$  radiation on an automatic diffractometer. The earlier results are confirmed except for small changes in bond distances and bond angles. In both structures, the equatorial glycosidic C(1)–O(1) bonds are significantly short.

The crystal structure of  $\beta$ -D-glucose was determined by Ferrier (1963) and that of cellobiose by Jacobson, Wunderlich & Lipscomb (1961) and by Brown (1966). These structures have now been refined from new experimental data obtained on a Picker four-angle automatic diffractometer. The primary purpose of this refinement was to obtain bond distances with an accuracy comparable to those from other recent structure determinations of pyranose sugars (Berman, Chu & Jeffrey, 1967). The cell parameters, remeasured on the diffractometer, are given in Table 1. The corresponding calculated densities are in good agreement with the observed values previously reported.



Fig. 1. The structure of one asymmetric unit of  $\beta$ -D-glucose viewed down the *c* axis. The diagram is produced by *ORTEP* (Johnson, 1965).

H(C6-2)

0.271

0.196

-0.109

#### Table 1. Crystallographic data

Space group	$\beta$ -D-Glucose $P2_12_12_1$	Cellobiose P2 <sub>1</sub>
	9·205 + 0·004 Å	10·972 + 0·004 Å
b	12.640 + 0.005	13.048 + 0.005
с	$6.654 \pm 0.003$	$5.091 \pm 0.003$
β	· <b>–</b>	$90.83 \pm 0.05^{\circ}$
$D_x$	1.545 g.cm <sup>-3</sup>	1.560 g.cm <sup>-3</sup>

For  $\beta$ -D-glucose, 775 independent reflections with  $2\theta$  values below 130° were measured, of which 716 reflections had intensities significantly above the background. For cellobiose, 1239 of the 1257 independent reflections measured were significantly above background. In both cases, the intensity data were collected in two different quadrants of the reciprocal lattice and the arithmetic mean values were used.

The refinements were by the full-matrix least-squares IBM 7090 program (Busing, Martin & Levy, 1962; Shiono, 1966) starting with the positional and thermal parameters of the carbon and oxygen atoms in  $\beta$ -Dglucose given by Ferrier (1963) and those of cellobiose given by Brown (1966). Cruickshank's (1961) weighting scheme was used in the refinement, except that zero weights were assigned to unobserved reflections. The atomic scattering factors used were those of Berghuis, Haanappel, Potters, Loopstra, MacGillavry & Veenendaal (1955). After two cycles of anisotropic refinement, the *R* values were reduced to 0.073 and 0.067 for  $\beta$ -Dglucose and cellobiose, respectively. All the hydrogen atoms were clearly revealed in difference Fourier syntheses, at reasonable positions with respect to the car-

#### Table 2. Fractional atomic coordinates and thermal parameters for $\beta$ -D-glucose

The estimated standard deviations are given in parentheses and refer to the last decimal positions of respective values. The expression for the temperature factor exponent consistent with the  $\beta$ -values is:

$-(\beta_{11}h^2+\beta_2)$	$k^{2} + \beta_{33}l^{2} + \beta_{33}l^{2}$	$2\beta_{12}hk + 2\beta_{12}$	$_{3}hl+2\beta_{23}kl$ ).
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	x	v	Z	$\beta_{11}$	β22	β33	$\beta_{12}$	$\beta_{13}$	$\beta_{23}$
0(1)	-0.0611(3)	0.2279(2)	0.5825(4)	0.0147(3)	0.0055(2)	0.0203(6)	0.0001(2)	0.0017(4)	-0.0037(3)
O(1)	-0.0011(3)	0.0060(2)	0.5587(4)	0.0155(4)	0.0042(1)	0.0235(6)	0.0002(2)	0.0051(4)	0.0031(3)
O(2)	-0.1119(3)	0.0000(2)	0.3307(4)	0.0133(4)	0.0072(1)	0.0214(7)	0.0002(2)	0.0037(4)	-0.0010(3)
O(3)	-0.1147(3)	-0.0647(2)	0.1445(4)	0.0120(3)	0.0028(1)	0.0314(7)	-0.0007(2)	-0.0037(4)	-0.0010(3)
O(4)	0.1297 (3)	0.0173 (2)	-0·0825 (4)	0.0146 (4)	0.0060(2)	0.0264 (/)	0.0009(2)	0.0060(4)	-0.0045 (3)
O(5)	0.0636 (3)	0.2220(1)	0.2893 (3)	0.0113 (3)	0.0032 (1)	0.0165 (5)	-0.0005(2)	0.0013(3)	-0.0000 (2)
O(6)	0.0992(3)	0.2936(2)	-0.1079 (4)	0.0188 (4)	0.0040(1)	0.0192 (6)	-0.0013(2)	-0.0029(4)	0.0010 (2)
ciú	0.0198(4)	0.1614(2)	0.4610(5)	0.0109 (4)	0.0040(2)	0.0166(7)	-0.0006(2)	-0.0001(5)	0.0008(3)
$\tilde{C}(2)$	-0.0786(4)	0.0717(2)	0.3902(5)	0.0098 (4)	0.0034(2)	0.0184 (7)	-0.0002(2)	0.0000 (5)	0.0010 (3)
$\tilde{C}(3)$	-0.0081(4)	0.0059(2)	0.2259(5)	0.0097 (4)	0.0028(1)	0.0217 (8)	0.0001(2)	-0.0020(4)	-0.0003(3)
Č(4)	0.0486 (4)	0.0764 (2)	0·0600 (̀5́)	0.0100 (4)	0.0039 (2)	0.0171 (7)	0.0007 (2)	0.0013 (5)	-0.0015 (3)
C(5)	0.1479 (3)	0.1614(2)	0.1486 (5)	0.0088 (4)	0.0039 (2)	0.0205 (8)	0.0001 (2)	0.0007 (5)	0.0001 (3)
C(6)	0.2099 (4)	0.2385 (3)	-0.0027(6)	0.0117 (4)	0.0055 (2)	0.0238 (9)	-0.0011 (3)	0.0041 (6)	0.0010 (4)
H(01)	0.010	0.252	0.676						
H(O2)	-0.212	0.020	0.622						
H(O3)	-0.085	-0.128	0.188						
H(O4)	0.067	-0.002	-0.196						
H(O6)	0.085	0.370	-0.120						
H(C1)	0.116	0.137	0.540						
H(C2)	-0.175	0.104	0.337		•				
H(C3)	0.081	-0.035	0.296						
H(C4)	-0.041	0.107	-0.008						
H(C5)	0.238	0.125	0-218						
H(C6-1)	0.289	0.292	0.071						

bon and oxygen atoms. Two further cycles of leastsquares refinement, including all the hydrogen atoms, gave final R values of 0.043 for  $\beta$ -D-glucose and 0.037 for cellobiose. The positional parameters of the hydrogen atoms were not refined and the hydrogens were assigned the same thermal parameters as the carbon or oxygen atoms to which they are bonded. The final positional and thermal parameters are given in Tables 2 and 3. The observed and calculated structure factors are given in Tables 4 and 5.

The identification of the atoms and the illustration of the thermal ellipsoids (Johnson, 1965) are shown in Figs. 1 and 2. The bond lengths and bond angles, with their standard deviations, are given in Tables 6 and 7. The mean C-C bond length is 1.520 Å ( $\sigma$ =0.0018), for  $\beta$ -D-glucose and 1.522 Å ( $\sigma$ =0.0016) for cellobiose. The mean C–O bond lengths, excluding the ring oxygen and anomeric carbon atoms, are 1.425 ( $\sigma$ =0.0021) and 1.420 Å ( $\sigma$ =0.0017) for  $\beta$ -D-glucose and cellobiose, respectively. In both structures, the equatorial glycosidic C(1)–O(1) bonds are shortened by 5 to 10 $\sigma$ , which is in agreement with the observations made on other  $\beta$ -pyranosides (Chu & Jeffrey, 1967; Berman, Chu & Jeffrey, 1967). Apart from changes in individual bond distances and angles (up to 0.06 Å and 3° in cellobiose, and 0.02 Å and 2° in  $\beta$ -D-glucose), the structures are unchanged from those previously reported.

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### Table 3. Fractional atomic coordinates and thermal parameters for cellobiose

Estimated standard deviations and temperature factor expression are as in Table 2.

	x	v	z	<b>B</b> 11	B22	B 3 3	B12	<i>B</i> 13	<i>B</i> 23
<b>O</b> (1)	0.1955(2)	0.0000	0.3013(4)	0.0039(2)	0.0025(1)	0.0210(8)	0.0006 (1)	-0.0025(3)	0.0003 (3)
$\tilde{0}(2)$	0.1551(2)	-0.2025(2)	0.4254(5)	0.0048(2)	0.0023(1)	0.0306(10)	-0.0017(1)	-0.0043(3)	0.0003(3)
O(3)	0.3456(2)	-0.3075(2)	0.7189(5)	0.0054(2)	0.0074(1)	0.0316(10)	-0.0017(1)	-0.0043(3)	0.0012(3)
O(3)	0.4967(2)	-0.1753(2)	1.0242(5)	0.0034(2)	0.0024(1)	0.0310(10) - 0.0350(0)	-0.0001(1)	-0.0003(3)	0.0013(3)
O(5)	0.3607(2)	-0.0049(2)	1.0343(3)	0.0038(2)	0.0044(2)	0.0250(9)	0.0001(1)	-0.0023(3)	0.0038(3)
	0.5092(2)	0.1229(2)	0.7371(4)	0.0041(2)	0.0028(1)	0.0230(9) = 0.0200(10)	-0.0003(1)	-0.0031(3)	0.0010(3)
C(1)	0.2517(3)	0.1338(3)	0.5250(6)	0.0087(3)	0.0027(1)	0.0309(10) - 0.0312(11)	-0.0010(2)	-0.0028(4)	-0.0011(3)
C(1)	0.2517(3)	-0.0409(3)	0.3239(0)	0.0032(2)	0.0028(2)	0.0213(11)	0.0004(2)	-0.0018(4)	0.0003(4)
C(2)	0.2004(3)	-0.1000(3)	0.4883(0)	0.0039(2)	0.0032(2)	0.0185(11) - 0.0221(12)	-0.0003(2)	-0.0014(4)	-0.0001(3)
C(3)	0.3292(3)	-0.14392(3)	0.7952(6)	0.0035(2)	0.0027(2)	0.0231(12)	0.0004(2)	0.0004(4)	0.0002(4)
C(4)	0.4300(3)	-0.1438(3)	0.7848(6)	0.0035(2)	0.0031(2)	0.0180(11)	0.0002(2)	-0.0013(4)	0.0010(3)
C(5)	0.4330(3)	-0.0273(3)	0.7702(0)	0.0040(2)	0.0028(2)	0.0217(12)	0.0001(2)	-0.0028(4)	-0.0002(4)
	0.0128(3)	0.0277(3)	0.7793(7)	0.0051(3)	0.0034(2)	0.0354(15) - 0.0204(11)	-0.0007(2)	-0.0020(3)	0.0008(5)
O(2')	-0.0138(2) 0.2471(2)	0.3360(3)	-0.0007(0)	0.0034(2)	0.0037(1)	0.0394(11)	0.0007(1)	-0.0024(4)	0.0032(3)
O(2')	0.2471(2) 0.3425(3)	0.1042(3)	-0.0377(0)	0.0043(2)	0.0040(2)	0.0392(13)	0.0002(2)	0.0002(4)	0.0089(4)
O(5')	-0.0263(2)	0.2036(3)	0.1872(6)	0.0030(2)	0.0033(2)	0.0210(24) = 0.0210(0)	-0.0023(2)	-0.0143(0)	0.0140(0)
O(6')	-0.1830(2)	0.2030(2)	0.7478(5)	0.0034(2)	0.0028(1)	0.0510(9)	0.0000(1)	0.0000(3)	0.0014(3)
CUY	0.0449(3)	0.271(3)	0.2428(0)	0.0033(2)	0.0037(2)	0.0310(13) = 0.0310(13)	-0.0001(1)	-0.00023(4)	-0.0031(4)
C(2')	0.1711(3)	0.2807(3)	0.1365(7)	0.0040(2)	0.0033(2)	0.0319(12)	-0.0003(2)	-0.002(4)	0.0030(4)
C(3')	0.2311(3)	0.1769(3)	0.1783(8)	0.0042(2)	0.0033(2)	0.0340(14) = 0.0410(15) =	-0.0002(2)	-0.0024(4)	0.0023(4)
C(4')	0.1481(3)	0.1029(3)	0.3256(6)	0.0037(2)	0.0035(2)	0.0749(12)	0.0003(2)	-0.0016(4)	0.00033(4)
$\tilde{C}(5')$	0.0188(3)	0.1006(3)	0.2101(6)	0.0041(2)	0.0025(2)	0.0270(12)	0.0007(2)	-0.0011(4)	-0.0011(4)
Č(6')	-0.0702(3)	0.0438(3)	0.3772(7)	0.0038(3)	0.0034(2)	0.0393(15) =	-0.0002(2)	-0.0003(5)	-0.0003(4)
H(O2)	0.112	-0.214	0.593	0 0000 (0)	0 000 (2)	0 0070 (10)	0 0002 (2)	0 0005 (5)	0 0005 (1)
H(O3)	0.382	-0.312	0.564						
HÌO4)	0.585	-0.195	1.028						
H(O6)	0.545	0.170	0.886						
H(C1)	0.205	-0.025	0.690						
H(C2)	0.320	-0.170	0.320						
H(C3)	0.270	-0.180	0.865						
H(C4)	0.510	-0.170	0.640						
H(C5)	0.385	0.002	0.942						
H(C6-1)	0.610	-0.005	0.640						
H(C6-2)	0.590	0.000	0.970						
H(O1')	-0.040	0.370	-0.185						
H(O2')	0.216	0.393	-0.112						
H(O3')	0.375	0.140	0.420						
H(O6')	-0.230	0.084	0.200						
H(Cl')	0.055	0.245	-0.192						
H(C2')	0.165	0.318	0.315						
H(C3')	0.255	0.140	0.000						
H(C4')	0.140	0.120	0.515						
H(CS')	0.030	0.065	0.025						
H(C6'-1)	) - 0.028	0.080	0.540						
H(C0-2	1-0.025	-0.020	0.440						

# Table 4. Observed and calculated structure factors for $\beta$ -D-glucose The running index is k; other columns are $|F_{obs}|$ , $|F_{cale}|$ , A, B (×10).

2 4 8 10 12 14	L= 0 H= 0 50 59 50 876 90R 90H 10+ 7 7 56 62 62 67 70 70 162 169 169 213 226 22H L= 1 H= 1 36 62 0		157     557     0       1n2     186     0       n1n2     186     0       57     51     0       57     51     0       160     178     0       118     174     0       111     13     0       106     106     102     0       30     33     0     0	557 0 1'Ho- 1 40- 2 51 3 178 4 174 5 13- 102 0 33- 1	>4 55   >7 32   77 74   60 60   28 78   39 39   19 15   L- 0   872 945   619 645	0 55 6- 32- 20- 72- 59- 11- 25 12- 37 12- 3- 15 445 0 645- 0	3 4 5 4 6 6 7 2 8 5 0 2 1 4 2 5	4 93 7 4 80 66- 0 42 16- 19 71 31 1 23 17 19 35 19- 19 35 19- 19 27 0 19 27 0 19 47 45- 14 85 21-	93 45- 1 38- 2 64 15 4 29- 9 27- 1 14 2 83-	44 50 26 2 41 4 55 5 44 4 22 1 20 1 5 5 5 5 5 44	50 50 50 51 50 50 50 50 50 50 50 50 50 50	0 22 34- 41 47 1 7 24
2 3 4 5 6 7 8 9 10 11 12 13	210     243     243       160     135     0       377     396     356       38     33     0       27     29     29-       27     25     0       129     126     126       110     1     0       120     7     7-       104     107     0       37     34     0	135-13 0 14 33- 0 0 25 1 0 2 11- 3 0 4 109 5 39 7	12*     9     0       12*     9     0       204     204     0       1*     1**     1       155     318     20     249       318     202     249     247       313     320     249     318       216     215     319     338       216     267     247       352     342     342       176     167     347       39     36     35	204 4 5 479 4 196- 7 201 6 24- 9 102- 10 14- 11 107- 12 6 13	21 28 238 201 83 85 24 21 158 153 30 2µ 37 37 73 73 73 73 70 64 53 53	20- 20- 21- 21- 27- 0 0 27- 0 0 27- 0 0 0 0 0 0 0 0 0 0 0 0 0	3 6 4 3 5 2 1 26 2 17 3 3 4 2 5 7 6 11 7 14	0 60 43- 6 37 23 23 4 23 23 2 23 23 2 251 0 6 27 0 3 25 0 6 62 0 7 114 0 6 199 0	41- 30- 1- 291- 167 25- 114 149 149-	21 22 59 5 10• 1 29 2 27 2 431 43 37 5 295 29 39 4 39 4 39 4 39 4 39 4 39 4 39 4 39	0 0 7 34- 6 10- 2 19 8 + 4 0 430- 0 50- 0 290- 4 43- 1 27- 1 27- 1 27-	20-13-24-11-080000
14 01 2 3 4 5 6 7 8	46 50 50- L 2 H= 0 430 416 416 261 280 0 8 2 2- 147 171 0 104 92 92 145 145 0 21 16 16 132 136 0 45 51 51	0 10 2A0 11 0 12 171- 13 0 14 145 0 0 136- 1 0 2	1     105     105     52-       136     133     132-       56     56     4-       .	91- 14 11- 58- 0 78 1 45 2 13 3 82 4 5 0 6 8- 7 213 8	127 125 L= 11 844 900 446 472 147 149 503 512 475 468 361 342 212 197 37 35 154 154	125 0 	9 5 10 5 11 1 12 8 13 3 14 1 0 15 1 23 2 21 3 18	5 49 0 4 54 0 2* 1 0 9 85 0 0 31 0 8 13 0 8 13 0 1 1 1 1 = 3 2 158 0 5 242 98∞ 6 217 145∞ 7 190 163	49- 6 54- 1 85- 9 31- 10 13- 11 158 13 221- 162 6 58 1	59 5, 37 3 84 8 122 11 35 3 52 4 25 2 55 6 142 15 66 7	6 54- 8 38- 1 Pl 5 115 4 34- 7 27 0 60 1 H+ 4 0 5 15	000000
9 10 11 12 13 14 1 23 4 5	16 24 0   25 22 22   12* 1 0   84 92 92   50 9   26 19 19-   100 98 0   120 121 121-   56 50 0   100 98 0   100 78 8   100 8 8	24 3 0 4 1 5 0 6 50 7 0 8 9 9 4 10 9 9 11 52 12 0 13	410 409 376 410 409 376 5410 409 376 56 59 23 9 95 92 91 175 78 36 107 105 95- 118 120 73 13* 7 5 57 57 54 73 76 78- 4 13 4 18	40 9 160 10 101- 11 54- 12 14- 13 70 14 45- 55- 0 5- 1 20- 2 1- 3 24 4	183 186 125 126 87 88 78 75 38 33 6 54 19 127 374 370 111 104	194- 104- 24- 124 44 76 14 74 25- 52 	4 46 5 15 6 14 7 6 8 11 9 7 10 13 11 8 12 3 13 4 14 4	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	249 2 114- 3 106 4 59 5 115 6 9- 1 108 9 12 10 27 11 38 12	59 e 174 17 255 24 255 24 121 11 179 17 98 9 150 14 74 7 86 8 23 11	1 33- 122 7 239- 3 167- 3 49- 49- 138 2 63- 5 140- 5 140- 5 15- 10-	51 124 61 176 101- 107- 67- 41- 76 47- 1-
67 8 9 10 11 12 13 0 1	158 162 162 166 161 0 12, 14 14 67 67 0 247 246 246 46 44 0 27 24 24 65 67 0 18 167 177- 15 22 0	161_ 0 161_ 0 167- 2 0 3 44- 4 0 5 67- 6 7 0 6 22- 9	L= 3 ++ 1 + 415 421 0 + 415 421 0 + 149 150 139 = 143 201 133 83 87 80- 549 549 115 - 22 21 6- 169 163 41- - 209 201 200- 205 266 105 112 115 114	421- 6 54 7 146 8 35- 9 536- 10 70 11 157- 12 20 13 244- 19- 0	99 89 22 21 87 M1 147 148 85 85 226 229 13* 10 99 95 37 31 L# 3 H	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 51 1 4 2 15 3 7 4 30 5 34 6 12 7 10 8 7 9 10 10 12	8 534 534 0 40 36- 7 154 122- 9 369 364 3 340 253- 5 113 58 2 101 27 1 77 72 0 154 28 6 127 73	0 17- 0 93 1 49 2 59- 3 227- 4 97- 5 98 6 29 7 152- 9 204- 9	Le 75 7 197 26 268 26 312 309 30 175 17 155 14 122 12 142 13 84 8	11-   101   259-   236-   213-   107-   109-   136-   136-	33- 0 8A- 63- 193 723- 52- 9- 56 19 62
23456789101112	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	0 10 21- 11 0 12 12 12 176- 0 176- 0 175- 0	1     133     95_       70     41     55-       52     60     11-       30     31     24-       1     135     132     132       112     113     98-       72     75     49       44     80     63       135     139     108       134     134     108	168- 1 20 2 54 3 14- 4 56 7 57 8 44- 9 87- 10 12 11	23 16 165 164 167 166 198 197 143 142 136 140 29 25 64 67 98 101 125 127 34 33	9 13- 119- 112 149 73 84- 178 138- 34 57 128- 19- 16- 48- 46 73- 70- 127 10 33- 7	11 6 12 6 13 4 0 8 1 8 2 14 3 7 4 13 5 5 5 5	2 82 42- 6 89 65- 1 93 05- 1 93 0 8 87 74 9 147 82 1 67 0 8 135 133 1 53 53- 6 56 18-	70 10 23- 11 34- 12 13 93 46 0 123 1 67- 2 18- 3 54 55	166 16 76 2 1A 11 30 2 28 2 76 8 27 20 127 120 110 100 82 8	2 130- 23 16- 12- 12- 16- 12- 10- 10- 10- 10- 10- 10- 10- 10	108 14 7- 25- 29 53 4- 128- 16- 28-
1234567890	La 5 Pa 0 57 54 0 55 54 54- 57 54 0 67 54 54- 52 53 0 20 e 8- 62 el 0 20 19 13 31 31 0 62 65 65	54- 7 54- 7 54 9 54 9 51 11 61 12 61- 8 0 31 1 0 2	153     153     145       200     204     122       9x     101     45       50     48     24       30     38     34       45     46     11       24     26     23       L     5     5       28     24     0       42     37     36       66     61     28	49 17 164- 13 55- 39 0 16 1 45- 2 12- 3 4 24- 5 7- 6 54- 7	21 24 45 46 10* 13 45 46 58 66 67 73 53 48 54 53 123 124 175 174	4- 23 12- 44- 13- 0 31 34 67 21 67 29- 30- 38 31- 43 124 2 103 139-	7 5 8 8 9 7 10 6 11 6 12 3 0 5 1 10 2 4 3 10	4 58 51- 4 84 80 0 71 54- 7 72- 2 66 9- 3 13 31- L= 4 F= 3 8 59 59 4 109 57- 6 45 0 3 104 45	27 6 24- 7 46- 7 66 10 10 11 12 93 0 45 1 93- 2	12+ 1 77 3 H8 8 12+ 5 12+	9- 19- 25- 19- 19- 7- 282 282 42- 19	10- 100 32 0 5- 74-
11 0 1 2 3 4 5 6 7 8	63     60     0       L     6     H=     0       132     132     132       30     34     0       62     60     60       174     170     0       111     104     104-       77     si     0       53     54     0       13     24     22-	e0- 3 0 5 34 6 0 7 170 7 170 7 0 7 170 7 0 11 57 0 0	45     44     7-       h1     85     63       41     41     30       47     34     35       53     50     31-       35     37     26       36     30     21-       30     20     30       31     30     26       37     36     36       31     30     26       31     30     36	43 8 67- 9 26- 10 1 11 39 12 26- 7 0 1+ 1 24- 2 3 0 4	120 118 68 66 37 37 51 51 34 34 267 261 116 115 71 97 102 107 105 105	30 114 11- 65 21 29 12 49- 28 20 0 261- 92- 69- 76- 75 9 105-	4 12 5 6 6 16 7 19 8 12 9 1 10 3 11 2 0 22 1 7	2 128 123 3 67 63- 1 158 154 2 148 26 8 134 98 1 29 28 7 31 8- L+ 5 H+ 3 2 222 0 6 80 45	34- 3 72 4 32- 5 186- 6 51 7 2- 8 5- 9 30- 10 11 222 67- 0	28 24 63 55 83 86 51 54 66 64 59 54 26 26 30 11 233 234	20- 45 5 20 15- 16 15- 27 4 0	13 32- 86- 50- 65- 51 52- 21 71- 234-
4 123456 1	14+ 7 0 4- 7 F1 0 44 96 0 15+ 15 15- 17 17 17 10- 1 15 13 13 1- 0 F1 1 135 341 0	7 1 10 3 0 4 121- 5 0 6 1- 7 0 7 141-	24 27 27 27 14 16 10 109 109 37 10 109 37 109 25 10 109 10 109 109 10 109 10 100 10 100 100 100 100 100 100 100 100 100 100 100 100 100 1000 10	5	27 29 16 14 71 75 30 35 11* 7 55 57 L* 6 H 111 127 61 54 75 77	29 2 10- 9 73 17 25- 24 5- 5- 32 47- 127- 0 47- 35 20 72	2 10 3 8 5 4 5 4 11 7 6 8 4 9 1 10 3	9 111 76 9 88 79 1 53 49 8 46 17 3 122 83 7 50 0 37 36- 8 17 17 8 36 36 L= 6 H= 3	81 1 38 2 19 3 43- 4 90 5 27 6 8 7 2 8 0 9	107 104 120 124 46 59 125 121 31 31 66 70 37 31 52 46 24 22	94- 25 6H 13- 0 37 48- 13	48 10 49- 103- 28 70 2 2 18

•

Table 4 (cont.)

L= 6 H= 4 1 85 98 62	44 1 105 114 80- 82-	9 24 28 27 7- 7	15 15 15 S
1 11* 17 13 10 3 69 73 19-	4 2 131 136 2 138-	10 20 20 27- 0 4	34 48 40 7- L∓ 4 ⊱∎ 8
2 27 26 1 26 4 44 47 39-	27 4 87 81 72 36	0 11 0 0 0 0	15 13 13- 0
4 56 55 47 29- 6 12. 20 12-	16- 6 39 42 A 42-	2 190 190 14- 189- 2	40 41 32 26
5 16 19 16- 9 7 26 28 4	26-7 31 28 3 28-	3 48 48 47 8- 3	20 15 1 15
7 13 33 5 32- 4 36 31 30	6 9 30 33 32 10	57 52 52- 4 5	29 31 7 31-
L= 7 Ht 4 10 35 35 34-	9 10 36 31 29- 11-	6 29 29 27- 12- 6	28 24 24 3
1 34 35 25- 4- 0 132 125 0	125 0 101 106 106 0	R 25 30 20 4- 0	4. 4 0 4
2 34 33 33- 2- 1 107 109 8	108- 1 167 169 145- 86-	g 31 24 8 23 1	26 28 25 11-
		0 32 33 33- 0	17 16 1- 16
1 10 - 2 0 2 - 4 39 41 22-	35 4 81 83 38 74-	1 83 87 83 26- 1	76 72 0 72
3 11+ 16 0 16- 6 60 63 43	AA 6 42 44 3- 44-	3 37 41 40- 5- 3	42 46 0 46-
4 56 59 0 59- 7 40 41 40	9- 7 11+ 14 10- 10-	4 76 76 49- 58 4	19 12 0 12-
5 66 63 0 63- 8 71 69 67- 6 66 39 0 39 L= 6 H= 5	16 8 28 22 21- 6 9 44 45 7- 45-	5 20 19 14 13 5	12* 4 0 4-
7 121 120 0 120- 0 10+ 12 12	0 L= 5 H= 6	7 38 34 3 34 7	11. 4 0 4
9 12 9 0 9 2 44 47 42	22 0 11 2 0 2-	8 21 19 19- 6 8 18 5 H= 7	72 73 0 73
10 43 43 0 43- 3 40 38 24	29 2 22 24 10 22	0 21 23 0 23- 0	23 20 0 20-
11 30 24 0 24- 4 31 35 15 12 21 27 0 27- 5 34 37 12	32 3 95 94 76 55- 35 4 25 19 8 18	1 34 33 23- 24- 1 2 21 22 12 18- 2	30 24 14- 24- 48 40 7 47
13 27 23 0 23 6 28 28 24-	15 5 24 13 2 13-	3 40 37 7 36- 3	38 37 • 16-
0 72 67 0 67 0 209 205 205-	0 7 10 13 13 3-	5 19 10 0 10- 5	20 19 5 18
1 124 119 39 113- 1 21 14 14	0 L= 6 += 4	L+ 0 H+ 0 6	11. 15 1. 5
3 163 154 0 154 3 79 80 80	0 1 30 25 20- 16-	1 12. 6 6. 0	43 40 36- 16- La 2 He e
4 146 140 62- 126 4 104 103 103-	0 2 27 28 25- 12-	2 174 175 175 0 0	12- 3 3- 0
6 204 145 25- 193 6 210 210 210	0 4 26 26 0 26-	4 12 12 12 0 2	63 63 62 9
7 111 104 72- 76 7 87 88 88	0 L= 0 H= 7	5 54 56 56 0 3	12 23 23 5
9 142 137 136 20- 9 12- 5 5.	9 2 12 16 0 16-	7 60 55 55- 0 5	28 32 20 26
10 99 95 14 94 10 29 37 37-	0 3 37 35 0 35-	8 32 29 29 0 6	28 21 16- 14
12 49 50 47 18 12 60 59 59	0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	9 11• 3 3- 0 7	23 15 15 4-
	6 87 89 0 89-	0 51 52 0 52- 0	27 31 0 31-
1 123 121 120- 16 1 75 79 74-	26 8 193 190 Q 190	2 56 60 40 44 2	97 95 31 89-
2 298 302 300- 30 2 96 93 2-	92- 9 52 54 0 54-	3 61 64 37 52- 3	36 36 34. 12-
4 121 121 4- 121- 4 37 37 14-	38 10 20 20 0 20- 34- 11 18 8 0 8	4 71 73 59 43- 4	48 50 49- 10-
5 157 153 140- 61- 5 88 96 13	95 L= 1 H= 7	6 50 52 51 12-	L= 4 H= 9
7 90 40 36- 82 7 117 112 111	16-1 92 97 72 66-	7 23 18 18 3- 0	23 27 27 0 56 56 38 41-
8 63 60 52 30- 8 119 116 96-	65- 2 23 30 18 24	9 66 65 62 18 2	31 32 1 32
10 21 18 18- 3- 10 66 68 15	66- 4 43 43 41 12-	0 124 5 5- 0 0	
11 70 65 6 64 11 52 56 49	28- 5 52 52 52 6	1 35 40 7 39 1	45 44 44- 0
La 3 Ma 5 La 2 Ma 6	7 30 25 25- 1	3 55 57 57- 4 3	34 40 40 0 46 45 45 0
0 140 139 0 139 0 40 37 37-	0 8 70 71 67 22	4 21 24 12 21 4	33 40 40 0
2 118 117 69- 94- 2 116 189 77-	77 10 11• 9 9- 1-	5 11 15 14 7- 5	23 27 27- 0
3 70 78 77 16- 3 68 75 74-	12 11 20 18 11- 14-	7 33 39 29- 25- 0	11. 15 0 15-
• VE 94 13 93 4 129 116 49- 5 71 68 49- 47- 5 36 45 5	105- Le 2 He 7 66- 0 128 131 131- n	8 32 33 6 33-1	17 20 19 5
6 103 96 43- 86 6 50 47 17-	44 1 79 76 31- 70	La 3 Ha 8 1	79 76 15 75-
7 12+ 14 14- 2 7 30 28 13-	25 2 101 99 98- 8	0 56 52 0 52- 4	42 43 2- 43
9 31 31 12- 28- 9 43 39 5	39- 4 55 50 38- 33-	2 54 54 16 52	(L+ 2 H+ 10
10 38 38 1 38 10 39 40 40- 11 17 14 13- 2 11 65 66 63		3 43 34 11 33 0	
L+ 4 H+ 5 L+ 3 H+ 6	7 46 40 9- 39	5 39 44 44 1 2	55 56 56- 4
<b>U</b> 114 113 113- 0 0 28 32 0	32 A 32 36 34 L1	6 17 19 4- 19- 3	41 45 25 37



Fig. 2. The structure of one asymmetric unit of cellobiose viewed down the *c* axis. Dotted line is intramolecular hydrogen bond. The diagram is produced by *ORTEP* (Johnson, 1965).

# Table 5. Observed and calculated structure factors for cellobioseColumns are as in Table 4.

# Table 5 (cont.)

Table 5 (cont.)

56789011 012345A7890 0123456789	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	57 57 55 41 41 32- 57 57 55 41 32 41 57 57 55 41 32- 57 57 55 41 32- 57 57 55 41 32- 57 57 55 41 32- 57 57 55 57 5	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	He     6     L*     -4       21     21     1     1       23     23     1     1       24     2     1     1       25     21     1     1       25     23     1     1       98     97     91     1       98     97     91     2       98     97     91     2       90     80     88     480       91     70     24-       14     70     24-       14     70     1       51     47     48       50     53     44       51     47     48       50     53     43       51     47     51       53     48     54       54     48     54       54     48     54       54     48     54       54     52     52       54 <t< th=""><th>0 1 25 4 34 4 32 5 69 6 16- 1 0 3 7 4 9- 5 6- 1 7 6 16- 1 7 6 16- 1 7 6 16- 1 7 6 16- 1 7 6 17 7 17 1 7 1 17 1</th><th><math display="block"> \begin{array}{c ccccccccccccccccccccccccccccccccccc</math></th><th>0 22 37 1 9 12- 2 2 4 2 7 2 - 4 2 7 2 - 17 - 12- 7 8 - 4 2- 7 7 1 - - 2 - - 7 1 - - - 2 - - - - - - - - - - - - - - -</th></t<>	0 1 25 4 34 4 32 5 69 6 16- 1 0 3 7 4 9- 5 6- 1 7 6 16- 1 7 6 16- 1 7 6 16- 1 7 6 16- 1 7 6 17 7 17 1 7 1 17 1	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0 22 37 1 9 12- 2 2 4 2 7 2 - 4 2 7 2 - 17 - 12- 7 8 - 4 2- 7 7 1 - - 2 - - 7 1 - - - 2 - - - - - - - - - - - - - - -
0	43 41 41_ 112 105 27-	0 2	95 96 62	73- 7	43 47 29-	30- 3	5. 7 7	1 1	49 49 38	31-
ż	74 74 64-	37- 4	119 119 96-	70 9	67 68 18	66 Q	42 45 45		36 36 24-	27-
4	15 16 0	16- 6	63 61 3 <sub>8</sub>	48- 11	53 50 50-	1- 2	38 40 29-	28- 5	18 21 20-	
5	51 52 31-	42- 7	65 68 58	32	H# 3 L# -4		63 62 Z	62- 6	, 71 70 66 7 33 30 27-	21
î	11 18 23-	75- 9	171 169 137-	98- 1	57 57 12	56 5	46 46 46-	-	N* 3 L+ -5	1.5-
0	63 60 60	0 10	57 60 60- H= 5 L= 4	, ,	19 8 1-	8 7	28 30 12	27- 1	133 132 115	65
Ļ	65 61 26	55 0	64 9 9-		26 29 28-	5 8 30-	40 9 8- Ha 114 5	4- 2	67 66 23	62
5	5. 8 0	d- 2	179 181 161	83 6	21 19 14	13- 0	125 123 123	0 4	5 6 3-	· 5-
5	52 52 48 90 88 RF-	20- 3	131 128 69 27 18 4	108 7	45 48 42	23 1 30- 2	21 21 15- 67 68 48-	48 6	3 77 80 23- 5 42 43 39-	76
	H= 11 L= -3		47 45 40-	22 9	43 46 43	17 3	13 15 13-	8- 7	72 69 61	32
ĩ	69 70 24	67 7	74 71 32	64	N= 4 L= -4	5	41 43 42	- a - c	08 69 69	0
٥	H4 0 L 4	0 9	81 82 RO	13- 0	71 67 67	82 7	4+ 2 1	1- 1	83 77 72-	26-
i.	135 134 45	126	H* 6 L* 4		101 106 80-	69- 8	17 18 18-	2- 3	56 55 23	50
2	70 75 11 122 11v 40	112 1	16 16 16- 97 98 96-	24 4	55 55 55- 65 66 17-	63 0	120 117 117	0 5	, 18 20 20- 5 43 42 38	20-
:	49 45 34-	30 2	58 65 43-	48 5	29 28 13-	25- 1	73 75 47	58- 6	50 48 17-	45
~	124 125 125	° 4	136 138 137-	12 7	55 55 54-	10 3	15 14 0	14- 0	87 89 89	0
	113 113 40	200 5	17 16 4-	15- 8	27 31 31-	30 5	39 37 22-	30 1	23 20 14-	14
	39 39 39	7- 7	67 61 39-	47 10	52 50 48-	13 6	15 8 0	8 3	24 21 20	7-
10	24 30 26- 59 58 37-	45 4	), 30 30- He / Le 4	· ·	55 53 53	。 '	>> >4 3¥ H≡ 3 L= 5	- · ·	37 35 2-	35-
	H= 1 L= 4	0 1	24 27 27-	0 1	50 54 47-	26 0	5. 10 10-	32	H" 6 L" -5	•
ĭ	74 61 59	55- 2	88 89 87	20- 3	98 98 59	78- 2	55 59 51	29 1	49 48 17-	45-
23	157 159 151-	51- 3	25 21 4-	31 5	60 61 38 63 65 57-	47- 3	60 54 54 14 15 6-	14- 3	24 24 9-	22-
	71 67 66-	13 5	84 81 3-	01- 6	24 23 5-	22 5	95 90 16	89- 4	42 40 36-	17
ŝ	73 77 68-	36 7	20 19 18	i- 6	15 13 6	12- 7	108 109 63	49 0	) 47 <sup>°°</sup> 44 <sup>°</sup> 44 <sup>°</sup>	0
7	69 71 65	21	H+ 8L+ 4	9	101 105 85	62-	Ha 4 La 5			

# Table 6. Bond lengths (including hydrogen bonds) and bond angles in $\beta$ -D-glucose

Estimated standard deviations in parentheses refer to the last decimal positions of respective values.

i	j	D(ij)	i	j	k	∠( <i>ijk</i> )
C(1)	C(2)	1·525 (4) Å	C(2)	C(1)	O(1)	108·2 (3)°
C(2)	C(3)	1.520 (4)	C(2)	C(1)	O(5)	108.5 (2)
C(3)	C(4)	1.511 (4)	O(1)	C(1)	O(5)	107.0 (2)
C(4)	C(5)	1.529 (4)	C(1)	C(2)	C(3)	$112 \cdot 1(3)$
C(5)	C(6)	1.513 (5)	C(1)	C(2)	O(2)	108.5 (3)
			C(3)	C(2)	O(2)	109.7 (3)
C(1)	O(1)	1.383 (4)	C(2)	C(3)	C(4)	110.5 (3)
C(2)	O(2)	1.429 (4)	C(2)	C(3)	O(3)	108.7 (3)
C(3)	O(3)	1.432 (4)	C(4)	C(3)	O(3)	109.1 (3)
C(4)	O(4)	1.419 (4)	C(3)	C(4)	C(5)	109.8 (3)
C(1)	O(5)	1.433 (4)	C(3)	C(4)	O(4)	111.1 (3)
C(5)	O(5)	1.437 (4)	C(5)	C(4)	O(4)	108.2 (3)
C(6)	O(6)	1.419 (5)	C(4)	C(5)	C(6)	115.0 (3)
			C(4)	C(5)	O(5)	107.6 (2)
O(1)	O(6)a	2.666	C(6)	C(5)	O(5)	107.1 (3)
O(2)	O(3)b	2.686	C(5)	C(6)	O(6)	111.9 (3)
O(2)	O(6)c	2.708				
O(3)	O(5)c	2.772	C(1)	O(5)	C(5)	112.7 (2)
		Sym	metry code			
		- x	v	z		
		a x	v	1 + z		
		$b - \frac{1}{2} - x$	$-\dot{y}$	$\frac{1}{2} + z$		
		c -x	$-\frac{1}{2}+y$	$\frac{\overline{1}}{2} - z$		

		D/m		ust decimat		respective valu
i	j	D(ij)	ĺ	j	k	∠(ijk)
C(1)	C(2)	1·525 (5) Å	C(2)	<b>C</b> (1)	<b>O</b> (1)	109·0 (3)*
C(2)	C(3)	1.520 (5)	C(2)	C(1)	O(5)	108.3 (3)
C(3)	C(4)	1.543 (5)	O(1)	C(1)	O(5)	107.4 (2)
C(4)	C(5)	1.532 (5)	C(1)	C(2)	C(3)	108.3 (3)
C(5)	C(6)	1.519 (5)	C(1)	C(2)	O(2)	110·0 (3)
			C(3)	C(2)	O(2)	113.6 (3)
C(1)	O(1)	1.397 (4)	C(2)	C(3)	C(4)	109.5 (3)
C(2)	O(2)	1.416 (4)	C(2)	C(3)	O(3)	112.0 (3)
C(3)	O(3)	1.427 (4)	C(4)	C(3)	O(3)	111.5 (3)
C(4)	O(4)	1.420 (4)	C(3)	C(4)	C(5)	111.0 (3)
C(1)	O(5)	1.425 (4)	C(3)	C(4)	O(4)	108.1 (2)
C(5)	O(5)	1.436 (4)	C(5)	C(4)	O(4)	109.4 (2)
C(6)	O(6)	1.416 (5)	C(4)	C(5)	C(6)	111.0 (3)
			C(4)	C(5)	O(5)	110·5 (3)
C(1')	C(2')	1.514 (5)	C(6)	C(5)	O(5)	105.4 (3)
C(2')	C(3')	1.519 (5)	C(5)	C(6)	O(6)	112.2 (3)
C(3')	C(4')	1.530 (5)				
C(4')	C(5')	1.527 (5)	C(2')	C(1')	O(1')	110.2 (3)
C(5')	C(6')	1.501 (5)	C(2')	C(1')	O(5')	109.3 (3)
			O(1')	C(1')	O(5')	107.0 (3)
C(1')	O(1')	1.381 (5)	C(1')	C(2')	C(3')	110.0 (3)
C(2')	O(2′)	1.423 (5)	C(1')	C(2')	O(2')	110.6 (3)
C(3')	O(3')	1.410 (5)	C(3')	C(2')	O(2')	106·5 (3)
C(4′)	O(1)	1.446 (4)	C(2')	C(3')	C(4')	111.8 (3)
C(1')	O(5′)	1.435 (4)	C(2')	C(3')	O(3')	107.1 (3)
C(5')	O(5′)	1.437 (4)	C(4′)	C(3')	O(3)'	112.5 (3)
C(6′)	O(6′)	1.423 (5)	C(3')	C(4')	C(5')	112.3 (3)
			C(3')	C(4')	O(1)	109.0 (3)
O(2)	O(1')a	2.766	C(5')	C(4')	O(1)	106.4 (3)
O(2)	O(5')b	2.733	C(4')	C(5')	C(6')	113.6 (3)
O(3)	O(6)c	2.711	C(4')	C(5')	O(5′)	109.2 (3)
O(3)	O(6')b	2.808	C(6')	C(5')	O(5′)	106.4 (3)
O(4)	O(6)c	2.807	· C(5')	C(6′)	O(6′)	111.8 (3)
O(4)	O(2')d	2.814				
O(5)	O(3')	2.767	C(1)	O(5)	C(5)	112.4 (2)
O(2')	O(6′)e	2.789	C(1)	O(1)	C(4')	116-1 (2)
			C(1')	O(5′)	C(5')	113.5 (3)
			Symmetry code			
		_	· · · · · ·	-		
			~ y	4		

Table 7. Bond lengths (including hydrogen bonds) and bond angles in cellobiose Estimated standard deviations in parentheses refer to the last decimal positions of respective values.

e -x  $\frac{1}{2}+y$ for providing the crystals of  $\beta$ -D-glucose and Dr R. CHU Rosenstein of this laboratory for making the crystals

а

b

с

d

-x

- x

1-x

1-x

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z

- z

- z

- z

-z

+y

+v

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